

Section A

(Attempt all questions of this section)

Question 1

- a. What quantity must be added to each term of ratio $m + n : m - n$ to make it equal to $(m + n)^2 : (m - n)^2$? [3]
- b. The catalogue price of a computer set is ₹ 45000. The shopkeeper gives a discount of 7% on listed price. He gives further off season discount of 4% on balance. However, Sales Tax at 8% is charged on the remaining amount. Find:
(i) Amt. of Sales Tax a customer has to pay.
(ii) Final price he has to pay for computer set. [3]
- c. If B and C are two matrices such that $B = \begin{bmatrix} 1 & 3 \\ -2 & 0 \end{bmatrix}$ & $C = \begin{bmatrix} 17 & 7 \\ -4 & -8 \end{bmatrix}$. Find the matrix A so that $BA = C$. [4]

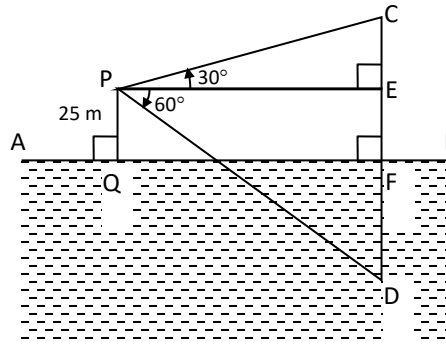
Question 2

- a. Mrs. Suneeta saves ₹ 8000 every year & invests it at the end of the year at 10% p.a. CI. Calculate her total savings at the end of third year. [3]
- b. Evaluate: $3 \cos 80^\circ \operatorname{cosec} 10^\circ + 2 \cos 59^\circ \operatorname{cosec} 31^\circ$. [3]
- c. In ΔPQR , L & M are two points on base QR, such that $\angle LPQ = \angle QRP$ & $\angle RPM = \angle RQP$. Prove that:
i) $\Delta PQL \sim \Delta RPM$
ii) $QL \times RM = PL \times PM$
iii) $PQ^2 = QR \times QL$ [4]

Question 3

- a. A company with 4000 shares of nominal value of ₹ 110 each declare an annual dividend of 15%. Calculate
i) Total amount of dividend
ii) Annual income of a person who holds 88 shares in the company.
iii) If he received only 10% on his investment, find the price for each share. [3]
- b. The marks of 20 students in a test were as follows:
2, 6, 8, 9, 10, 11, 11, 12, 13, 13, 14, 14, 15, 15, 15, 16, 16, 18, 19 & 20.
Calculate: (i) the mean, (ii) the median, (iii) the mode [3]

- c. The angle of elevation of a stationary cloud from a point 25 m above a lake is 30° and the angle of depression of its reflection in lake is 60° . What is the height of cloud above that lake-level? [4]



Question 4

- a. Given $A = \{x : -1 < x \leq 5, x \in \mathbb{R}\}$
 $B = \{x : -4 \leq x < 3, x \in \mathbb{R}\}$
 Represent on different number lines:
 (i) $A \cap B$ (ii) $A' \cap B$ (iii) $A - B$ [3]
- b. The length of common chord of two intersecting circles is 30 cm. If the diameters of these two circles be 50 cm & 34 cm. Calculate the distance between their centers. [3]
- c. Mr. Bhalu has a Savings Bank Account in Punjab National Bank. His pass book has following entries:

Date 1997	Particulars	Debit (₹)	Credit (₹)	Balance (₹)
April 1	B/F	-	-	3220.00
April 15	By.T.	-	2010.00	5230.00
May 8	To Cheque	298.00	-	4932.00
July 15	By Clearing	-	4628.00	9560.00
July 29	By Cash	-	5440.00	15000.00
Sep. 10	To Self	-	6980.00	8020.00
Jan. 10 (1998)	By Cash	-	8000.00	16020.00

Calculate the interest due to him at the end of 31st March 1998 at the rate of 6% p.a. [4]

Section B

(Attempt any four questions of this section)

Question 5

- a. The marks obtained by 120 students in a mathematics test are given below:

Marks	0-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80	80-90	90-100
No. of students	5	9	16	22	26	18	11	6	4	3

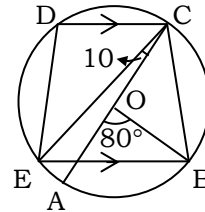
Use Ogive to estimate

- i) Median
 - ii) No. of students who scored more than 75% marks in a test
 - iii) The no. of students who did not pass in test if the pass percentage was 40
 - iv) The lower quartile [6]
- b. If $x = \frac{6ab}{a+b}$, find the value of: $\frac{x+3a}{x-3a} + \frac{x+3b}{x-3b}$. [4]

Question 6

- a. In the given figure, AC is diameter CD & BE is parallel. $\angle AOB = 80^\circ$, $\angle ACE = 10^\circ$. Calculate:

- i) $\angle BEC$
- ii) $\angle BCD$
- iii) $\angle CED$



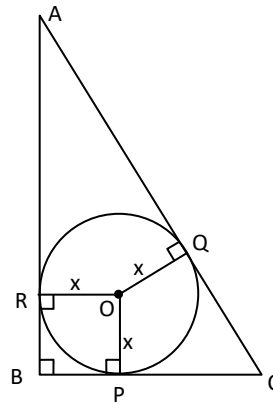
- b. The ratio of base area and curved surface area of a conical tent is 40: 41. If its height is 18 m. Find the air capacity of tent in terms of π . [3]
- c. Mr. Batliwala has a R.D. Account of Rs. 300 per month. If the rate of interest is 12% & the maturity value is Rs. 8100. Find the time (in yrs.) of this R.D. Account. [4]

Question 7

- a. Show that $2x + 7$ is a factor of $2x^3 + 5x^2 - 11x - 14$. Hence factorize the given expression completely, using factor theorem. [3]
- b. Prove that: $(\sin A + \operatorname{cosec} A)^2 + (\cos A + \sec A)^2 = 7 + \tan^2 A + \cot^2 A$. [3]
- c. If $A = \begin{bmatrix} a & 0 \\ 0 & 2 \end{bmatrix}$, $B = \begin{bmatrix} 0 & -b \\ 1 & 0 \end{bmatrix}$, $M = \begin{bmatrix} 1 & -1 \\ 1 & 1 \end{bmatrix}$ & $BA = M^2$, find values of a & b. [4]

Question 8

- a. ABC is a right angled triangle. AB = 12 cm, AC = 13 cm. A circle with centre O has been inscribed inside the triangle. Calculate the value of x, the radius of inscribed circle. [3]



- b. The diameter of a sphere is 6 cm. It is melted & drawn into a wire of diameter 0.2 cm. Find the length of the wire. [3]
- c. Mr. Ram Gopal invested ₹ 8000 in 7% ₹ 80. After a year he sold these shares at ₹ 75 each & invested the proceeding (including his dividend) in 18% ₹ 25 shares at ₹ 41. Find:
 i) Dividend for first year
 ii) Annual income in second year [4]

Question 9

- a. During every financial year, the value of a machine depreciates by 12%. Find the original cost of a machine which depreciates by Rs.2640 during second financial year of its purchase. [3]
- b. A open cylindrical vessel of internal diameter 7 cm & height 8 cm stands on a table. Inside this is place a solid metallic right circular cone, the diameter of whose base is $3\frac{1}{2}$ cm & height = 8 cm. Find volume of water required to fill the vessel. [3]
- c. A rectangular tank has length = 4 m, width = 3 m & capacity = 30 m³. A small model of tank is made with capacity 240 cm³. Find:
 i) Dimensions of model
 ii) Ratio between total surface area of tank and its model. [4]

Question 10

- a. Find the value of 'K' if (x – 2) is a factor of $x^3 + 2x^2 - kx + 10$. Hence determine whether (x + 5) is also a factor. [3]
- b. A manufacturer sells a washing machine to a wholesaler sells it to a trader at a profit of ₹ 1500 & trader in turn sells it to a consumer at a profit of ₹ 1800. If the rate of VAT is 8%, find:
 (i) Amount of VAT received by State Government on sale of this machine from manufacturer & the wholesaler.
 (ii) the amount the consumer pays for the machine. [3]
- c. The mean of following distribution is 62.8 and the sum of all frequencies is 50. Find the missing frequencies f_1 & f_2 . [4]

Class	0-20	20-40	40-60	60-80	80-100	100-120
Frequency	5	f_1	10	f_2	7	8

Answer key

Section A

(Attempt all questions of this section)

Question 1

- a. What quantity must be added to each term of ratio $m + n : m - n$ to make it equal to $(m + n)^2 : (m - n)^2$? [3]

Solution:

Let 'x' be added to each term of given ratio.

∴ According to given condition,

$$\frac{m + n + x}{m - n + x} = \frac{(m + n)^2}{(m - n)^2}$$

$$\therefore \frac{m + n + x}{m - n + x} = \frac{m^2 + 2mn + n^2}{m^2 - 2mn + n^2}$$

By Dividendo, we get,

$$\frac{m + n + x - (m - n + x)}{m - n + x} = \frac{m^2 + 2mn + n^2 - (m^2 - 2mn + n^2)}{m^2 - 2mn + n^2}$$

$$\frac{m + n + x - m + n - x}{m - n + x} = \frac{m^2 + 2mn + n^2 - m^2 + 2mn - n^2}{m^2 - 2mn + n^2}$$

$$\frac{2n}{m - n + x} = \frac{4mn}{m^2 - 2mn + n^2}$$

$$\therefore 2n(m^2 - 2mn + n^2) = 4mn(m - n + x)$$

$$m^2 - 2mn + n^2 = 2m(m - n + x)$$

$$\therefore m^2 - 2mn + n^2 = 2m^2 - 2mn + 2mx$$

$$m^2 - 2m^2 + n^2 = 2mx$$

$$\therefore n^2 - m^2 = 2mx$$

$$\therefore x = \frac{n^2 - m^2}{2m}$$

Required no. to be added is

$$\therefore x = \frac{n^2 - m^2}{2m}$$

- b. The catalogue price of a computer set is ₹ 45000. The shopkeeper gives a discount of 7% on listed price. He gives further off season discount of 4% on balance. However, Sales Tax at 8% is charged on the remaining amount. Find:
- (i) Amt. of Sales Tax a customer has to pay.
(ii) Final price he has to pay for computer set. [3]

Solution:

$$\text{Marked Priced (MP)} = ₹ 45000$$

$$\text{Discount } d_1 = 7\%$$

$$d_2 = 4\%$$

$$\text{Rate of ST} = 8\%$$

$$\begin{aligned} \text{Sale Price} &= \text{MP} \left(1 + \frac{d_1}{100}\right) \left(1 + \frac{d_2}{100}\right) \\ &= 45000 \left(1 + \frac{7}{100}\right) \left(1 + \frac{4}{100}\right) \\ &= 45000 \times \frac{93}{100} \times \frac{96}{100} \\ &= ` 9 \times 93 \times 48 \end{aligned}$$

$$\text{Sale Price} = ` 40,176$$

$$\begin{aligned} \text{i) Sales Tax (')} &= \frac{\text{Rate of ST}}{100} \times \text{SP} \\ &= \frac{8}{100} \times 40176 \end{aligned}$$

$$\text{Sales Tax (')} = ` 3214.08$$

$$\text{ii) Final price for computerset} = \text{SP} + \text{Sales Tax}$$

$$= 40176 + 3214.08$$

$$\therefore \text{Final Price} = ` 43390.08$$

- c. If **B** and **C** are two matrices such that $\mathbf{B} = \begin{bmatrix} 1 & 3 \\ -2 & 0 \end{bmatrix}$ & $\mathbf{C} = \begin{bmatrix} 17 & 7 \\ -4 & -8 \end{bmatrix}$. Find the matrix **A** so that $\mathbf{BA} = \mathbf{C}$. [4]

Solution:

$$\mathbf{B}_{2 \times 2} \cdot \mathbf{A}_{m \times n} = \mathbf{C}_{2 \times 2}$$

Using the rule for matrix multiplication

$$p \times q \cdot q \times r = p \times r$$

$$q = 2, \quad r = 2$$

$$\therefore \text{Order of matrix } \mathbf{A} = 2 \times 2$$

$$\text{Let } \mathbf{A} = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$$

$$\mathbf{BA} = \mathbf{C}$$

$$\begin{bmatrix} 1 & 3 \\ -2 & 0 \end{bmatrix} \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} 17 & 7 \\ -4 & -8 \end{bmatrix}$$

$$\begin{bmatrix} 1(a) + 3(c) & 1(b) + 3(d) \\ -2(a) + 0(c) & -2(b) + 0(d) \end{bmatrix} = \begin{bmatrix} 17 & 7 \\ -4 & -8 \end{bmatrix}$$

$$\begin{bmatrix} a + 3c & b + 3d \\ -2a & -2b \end{bmatrix} = \begin{bmatrix} 17 & 7 \\ -4 & -8 \end{bmatrix}$$

Since matrices are equal, their corresponding elements are equal,

$$a + 3c = 17 \quad \dots \text{ (i)}$$

$$b + 3d = 7 \quad \dots \text{ (ii)}$$

$$-2a = -4$$

$$\therefore a = 2$$

$$-2b = -8$$

$$\therefore b = 4$$

Substituting $a = 2$ in (i)

$$a + 3c = 17$$

$$2 + 3c = 17$$

$$3c = 17 - 2$$

$$3c = 15$$

$$\therefore c = 5$$

Substituting $b = 4$ in (ii)

$$b + 3d = 7$$

$$4 + 3d = 7$$

$$\therefore 3d = 7 - 4$$

$$\therefore 3d = 3$$

$$\therefore d = 1$$

$$\therefore A = \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} 2 & 4 \\ 5 & 1 \end{bmatrix}$$

Question 2

a. Mrs. Suneeta saves ₹8000 every year & invests it at the end of the year at 10% p.a. CI.

Calculate her total savings at the end of third year.

[3]

Solution:

For 1st year:

$$P = ₹ 0$$

$$R = 10\% \text{ p.a.}$$

$$T = 1 \text{ year}$$

$$I = \frac{P \times R \times T}{100} = ₹ 0$$

$$A = P + I + \text{savings}$$

$$= 0 + 0 + 8000$$

$$A = ₹ 8000$$

For 2nd year:

$$P = ₹ 8000$$

$$R = 10\% \text{ p.a.}$$

$$T = 1 \text{ year}$$

$$I = \frac{P \times R \times T}{100}$$

$$I = \frac{8000 \times 10 \times 1}{100} = ₹ 800$$

$$A = P + I + \text{savings}$$

$$= 8000 + 800 + 8000 = \text{`}16800$$

For 3rd year:

$$P = \text{`}16800$$

$$R = 10\% \text{ p.a.}$$

$$T = 1 \text{ year}$$

$$I = \frac{P \times R \times T}{100}$$

$$I = \frac{16800 \times 10 \times 1}{100} = \text{`}1680$$

$$A = P + I + \text{savings}$$

$$= 16800 + 1680 + 8000$$

$$A = \text{`}26,480$$

b. Evaluate: $3 \cos 80^\circ \operatorname{cosec} 10^\circ + 2 \cos 59^\circ \operatorname{cosec} 31^\circ$.

[3]

Solution:

$$\begin{aligned} & 3 \cos 80^\circ \cdot \operatorname{cosec} 10^\circ + 2 \cos 59^\circ \cdot \operatorname{cosec} 31^\circ \\ &= 3 \sin (90 - 80)^\circ \cdot \operatorname{cosec} 10^\circ + 2 \sin (90 - 59)^\circ \operatorname{cosec} 31^\circ \\ &= 3 \sin 10^\circ \cdot \operatorname{cosec} 10^\circ + 2 \sin 31^\circ \cdot \operatorname{cosec} 31^\circ \\ &= 3 \times 1 + 2 \times 1 \qquad \dots \sin \theta \cdot \operatorname{cosec} \theta = 1 \\ &= 3 + 2 \\ &= 5 \end{aligned}$$

c. In $\triangle PQR$, L & M are two points on base QR, such that $\angle LPQ = \angle QRP$ & $\angle RPM = \angle RQP$.

Prove that:

i) $\triangle PQL \sim \triangle RPM$

ii) $QL \times RM = PL \times PM$

iii) $PQ^2 = QR \times QL$

[2003]

Solution:

Given:

$$\angle LPQ = \angle QRP$$

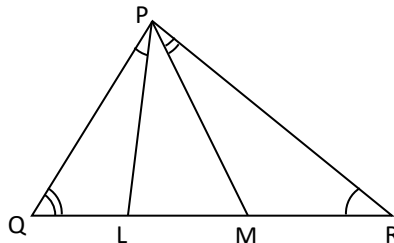
$$\angle RPM = \angle RQP$$

To prove:

i) $\triangle PQL \sim \triangle RPM$

ii) $QL \times RM = PL \times PM$

iii) $PQ^2 = QR \times QL$



Proof:

	Statement	Reason
1)	In $\triangle PQL$ & $\triangle RPM$, $\angle PQL = \angle RPM$ $\angle LPQ = \angle MRP$	Given Given
2)	$\triangle PQL \sim \triangle RPM$	By AA axiom of similarity

3)	$\frac{QM}{PM} = \frac{PL}{RM}$ $\therefore QL \times RM = PL \times PM$	c.s.s.t.p.
4)	In $\triangle PQL$ & $\triangle RQP$, $\angle PQL = \angle RQP$ $\angle LPQ = \angle PRQ$	Common angle Given
5)	$\triangle PQL \sim \triangle RQP$	By AA axiom of similarity
6)	$\frac{PQ}{RQ} = \frac{QL}{QP}$ $\therefore PQ \times PQ = QR \times QL$ $\therefore (PQ)^2 = QR \times QL$	c.s.s.t.p. hence proved

Question 3

- a. A company with 4000 shares of nominal value of ` 110 each declare an annual dividend of 15%. Calculate
- Total amount of dividend
 - Annual income of a person who holds 88 shares in the company.
 - If he received only 10% on his investment, find the price for each share. [3]

Solution:

Face Value (FV) = ` 110

Rate of dividend = 15%

No. of shares = 4000

Return % = 10%

i) Dividend = $\left(\frac{\text{Rate of dividend}}{\text{dividend}} \right) \times \text{FV} \times \left(\frac{\text{No. of Shares}}{\text{Shares}} \right)$
 $= \frac{15}{100} \times 110 \times 4000$

Dividend = ` 66000

ii) No. of shares = 88

Dividend = $\left(\frac{\text{Rate of dividend}}{\text{dividend}} \right) \times \text{FV} \times \left(\frac{\text{No. of Shares}}{\text{Shares}} \right)$
 $= \frac{15}{100} \times 110 \times 88$
 $= 33 \times 44$

Dividend = ` 1452

iii) Return% \times MV = Dividend% \times FV

$\frac{10}{100} \times \text{MV} = \frac{15}{100} \times 110$

$\text{MV} = \frac{15}{100} \times 110 \times \frac{100}{10}$

$$MV = \text{` } 165$$

b. The marks of 20 students in a test were as follows:

2, 6, 8, 9, 10, 11, 11, 12, 13, 13, 14, 14, 15, 15, 15, 16, 16, 18, 19 & 20.

Calculate: (i) the mean, (ii) the median, (iii) the mode

[3]

Solution:

$$i) \sum x = 2 + 6 + 8 + 9 + 10 + 11 + 11 + 12 + 13 + 13 + 14 + 14 + 15 + 15 + 15 + 16 + 16 + 18 + 19 + 20.$$

$$\sum x = 257$$

$$n = 20$$

$$\text{Mean} = \frac{\sum x}{n}$$

$$= \frac{257}{20}$$

$$\text{Mean} = \underline{12.85}$$

$$ii) N = 20 \text{ (even)}$$

$$\text{Median} = \frac{\left(\frac{n}{2}\right)^{\text{th}} \text{ term} + \left(\frac{n}{2} + 1\right)^{\text{th}} \text{ term}}{2}$$

$$= \frac{\left(\frac{20}{2}\right)^{\text{th}} \text{ term} + \left(\frac{20}{2} + 1\right)^{\text{th}} \text{ term}}{2}$$

$$= \frac{10^{\text{th}} \text{ term} + 11^{\text{th}} \text{ term}}{2}$$

$$= \frac{13 + 14}{2}$$

$$= \frac{27}{2}$$

$$\text{Median} = \underline{13.5}$$

$$iii) \text{ No. with highest frequency} = 15$$

$$\therefore \text{ Mode} = 15$$

c. The angle of elevation of a stationary cloud from a point 25 m above a lake is 30° & the angle of depression of its reflection in lake is 60° . What is the height of cloud above that lake-level? [4]

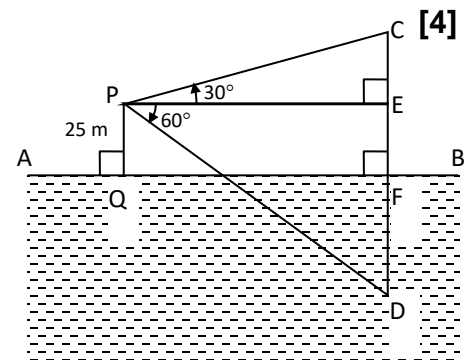
Solution:

AB = Lake level

PQ = 25 m

C = Stationary cloud

D = Image of cloud



$$\angle CPE = 30^\circ \text{ (Angle of elevation of S. cloud)}$$

$$\angle DPE = 60^\circ \text{ (Angle of depression of its reflection)}$$

From figure, $\square PQFB$ is a rectangle

$$\left. \begin{array}{l} PQ = EF = 25 \text{ m} \\ PE = QF \end{array} \right\} \text{ Opp. sides of rectangle are equal}$$

Also, $CF = DF$ (Laws of reflection)

In right $\triangle CEP$, In right $\triangle DEP$,

$$\tan 30^\circ = \frac{\text{Opp.}}{\text{Adj.}} \qquad \tan 60^\circ = \frac{\text{Opp.}}{\text{Adj.}}$$

$$\frac{1}{\sqrt{3}} = \frac{CE}{PE} \qquad \sqrt{3} = \frac{ED}{PE}$$

$$PE = \sqrt{3} \cdot CE \qquad PE = \frac{ED}{\sqrt{3}}$$

$$\therefore \sqrt{3} \cdot CE = \frac{ED}{\sqrt{3}}$$

$$\therefore ED = 3CE$$

$$\therefore EF + DF = 3[CF - EF] \qquad \dots \text{ (C-E-F) \& (E-F-D)}$$

$$\therefore 25 + CF = 3CF - 3 \times 25 \dots \text{ (DF = CF)}$$

$$\therefore 25 + CF = 3CF - 75$$

$$100 = 2CF$$

$$\therefore CF = 50 \text{ m}$$

Ans.: Height of cloud above lake level = 50 m.

Question 4

a. Given $A = \{x : -1 < x \leq 5, x \in \mathbb{R}\}$

$$B = \{x : -4 \leq x < 3, x \in \mathbb{R}\}$$

Represent on different number lines:

(i) $A \cap B$ (ii) $A' \cap B$ (iii) $A - B$

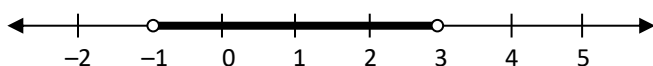
[3]

Solution:

i) For $A \cap B$:

$$\text{S.S.} = \{x : -1 < x < 3, x \in \mathbb{R}\}$$

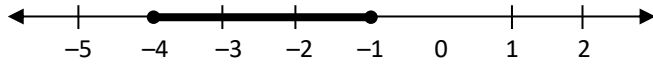
The graph of $A \cap B$ is:



ii) For $A' \cap B = B - A$:

$$\text{S.S.} = \{x : -4 \leq x \leq -1, x \in \mathbb{R}\}$$

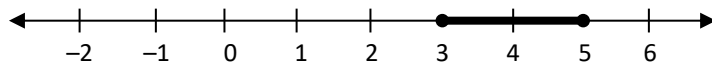
The graph of $A' \cap B$ is:



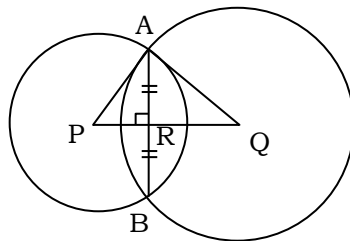
iii) For $A - B$:

$$\text{S.S.} = \{x : 3 \leq x \leq 5, x \in \mathbb{R}\}$$

The graph of $(A - B)$ is:



b. The length of common chord of two intersecting circles is 30 cm. If the diameters of these two circles be 50 cm & 34 cm. Calculate the distance between their centers. [3]



Solution:

Statement

1) $PQ \perp AB$

Reason

Line joining centres bisects the common chord Perpendicularly.

2) $AR = \frac{1}{2} AB = \frac{1}{2} \times 30$

from (1), substitution.

$\therefore AR = 15\text{cm}$

3) $AP = \frac{1}{2}(34) = 17\text{cm}$ $r = \frac{d}{2}$ & given

$AQ = \frac{1}{2}(50) = 25\text{ cm}$

4) In $\text{rt}\Delta ARP$,

$(AP)^2 = (AR)^2 + (PR)^2$ Pythagoras theorem

$\therefore (PR)^2 = (AP)^2 - (AR)^2$

$= (17)^2 - (15)^2$

from 2 & 3

$= 289 - 225 = 64$

Taking sq. root on both sides

$PR = 8\text{cm}$

5) In $\text{rt}\Delta ARQ$,

$(AQ)^2 = (AR)^2 + (RQ)^2$ Pythagoras theorem

$$\begin{aligned}
 &= (25)^2 - (15)^2 && \text{from 2 \& 3} && (RQ)^2 = (AQ)^2 - (AR)^2 \\
 & && && = 625 - 225 \\
 (RQ)^2 = 400 & && \text{Taking sq. root on both sides P - R - Q} \\
 & && RQ = 20\text{cm} \\
 6) PQ = PR + RQ & && P - R - Q \\
 & && = 8 + 20 \\
 & && \therefore PQ = 28 \text{ cm}
 \end{aligned}$$

- c. Mr. Bhalu has a Savings Bank Account in Punjab National Bank. His pass book has following entries:

Date 1997	Particulars	Debit (₹)	Credit (₹)	Balance (₹)
April 1	B/F	-	-	3220.00
April 15	By.T.	-	2010.00	5230.00
May 8	To Cheque	298.00	-	4932.00
July 15	By Clearing	-	4628.00	9560.00
July 29	By Cash	-	5440.00	15000.00
Sep. 10	To Self	-	6980.00	8020.00
Jan. 10 (1998)	By Cash	-	8000.00	16020.00

Calculate the interest due to him at the end of 31st March 1998 at the rate of 6% p.a. [4]

Solution:

Qualifying amount for various months:

Month	Principal
April, 1997	3220.00
May	4932.00
June	4932.00
July	4932.00
August	15000.00
September	8020.00
October	8020.00
November	8020.00
December	8020.00
January, 1998	16020.00
February	16020.00
March	+ 16020.00

Month	Principal
Total	₹ 113156.00

For Interest:

$$\text{Principal (P)} = ₹ 113156.00$$

$$\text{Rate (R)} = 6\% \text{ p.a.}$$

$$\text{Time (T)} = \frac{1}{12} \text{ yr.}$$

$$\begin{aligned} I &= \frac{P \times R \times T}{100} \\ &= \frac{113156 \times 6 \times 1}{100 \times 12} \\ &= \frac{56578}{100} \end{aligned}$$

$$\therefore I = ₹ 565.78$$

Section B

(Attempt any four questions of this section)

Question 5

a. The marks obtained by 120 students in a mathematics test are given below:

Marks	0-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80	80-90	90-100
No. of students	5	9	16	22	26	18	11	6	4	3

Use Ogive to estimate

- i) Median
- ii) No. of students who scored more than 75% marks in a test
- iii) The no. of students who did not pass in test if the pass percentage was 40
- iv) The lower quartile

[6]

Solution:

Marks	No. of Students f	Cumulative frequency c.f.	(x, y)
0-10	5	5	(10, 5)
10-20	9	5 + 9 = 14	(20, 14)
20-30	16	14 + 16 = 30	(30, 30)
30-40	22	30 + 22 = 52	(40, 52)

40-50	26	$52 + 26 = 78$	(50, 78)
50-60	18	$78 + 18 = 96$	(60, 96)
60-70	11	$96 + 11 = 107$	(70, 107)
70-80	6	$107 + 6 = 113$	(80, 113)
80-90	4	$113 + 4 = 117$	(90, 117)
90-100	3	$117 + 3 = 120$	(100, 120)

i) $N = 120$ (even)

$$\begin{aligned} \text{Median} &= \left(\frac{N}{2}\right)^{\text{th}} \text{ term} \\ &= \left(\frac{120}{2}\right)^{\text{th}} \text{ term} \\ &= 60^{\text{th}} \text{ term} \\ \text{Median} &= \underline{43} \end{aligned}$$

ii) No. of students scoring more than 75% marks = $120 - 110 = \underline{10}$

iii) No. of students who did not pass = 52

iv) Lower Quartile (Q_1) = $\left(\frac{N}{4}\right)^{\text{th}}$ term

$$\begin{aligned} &= \left(\frac{120}{4}\right)^{\text{th}} \text{ term} \\ &= 30^{\text{th}} \text{ term} \\ Q_1 &= \underline{30} \end{aligned}$$

b. If $x = \frac{6ab}{a+b}$, find the value of: $\frac{x+3a}{x-3a} + \frac{x+3b}{x-3b}$. [4]

Solution:

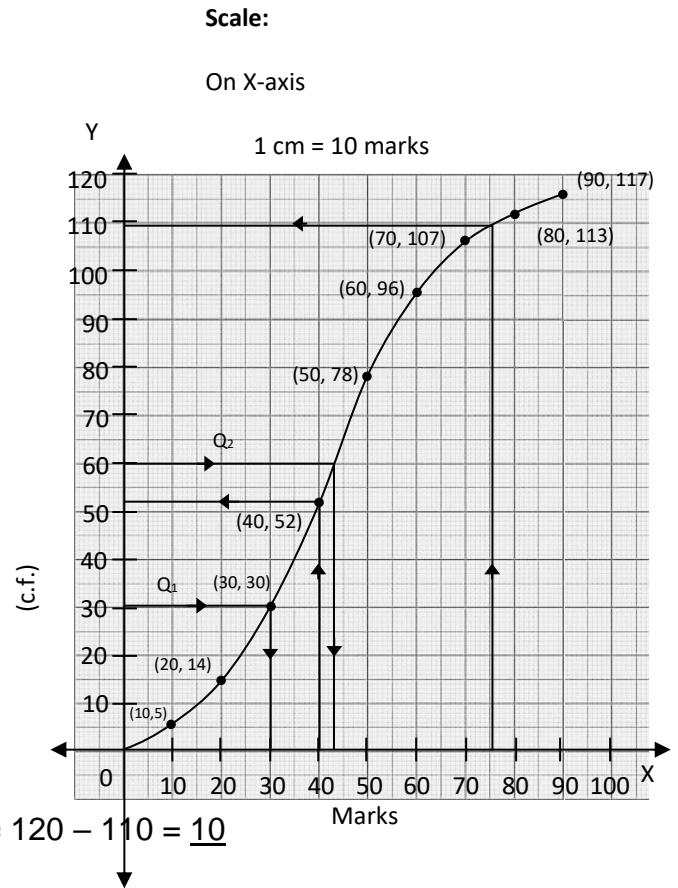
$$x = \frac{6ab}{a+b} \quad \dots \text{ given}$$

$$\therefore \frac{x}{3a} = \frac{2b}{a+b}$$

By Componendo-Dividendo, we get,

$$\begin{aligned} \frac{x+3a}{x-3a} &= \frac{2b+a+b}{2b-a-b} \\ \therefore \frac{x+3a}{x-3a} &= \frac{3b+a}{b-a} \quad \dots (i) \end{aligned}$$

$$x = \frac{6ab}{a+b} \quad \dots \text{ given}$$



$$\frac{x}{3b} = \frac{2a}{a+b}$$

By Componendo-Dividendo, we get,

$$\frac{x+3b}{x-3b} = \frac{2a+a+b}{2a-a-b}$$

$$\therefore \frac{x+3b}{x-3b} = \frac{3a+b}{a-b} \quad \dots \text{(ii)}$$

Add (i) & (ii), we get,

$$\begin{aligned} \frac{x+3a}{x-3a} + \frac{x+3b}{x-3b} &= \frac{3b+a}{b-a} + \frac{3a+b}{a-b} \\ &= \frac{3b+a}{b-a} - \frac{3a+b}{a-b} \\ &= \frac{3b+a-3a-b}{b-a} \\ &= \frac{2b-2a}{b-a} \\ &= \frac{2(b-a)}{(b-a)} \end{aligned}$$

$$\frac{x+3a}{x-3a} + \frac{x+3b}{x-3b} = 2$$

Question 6

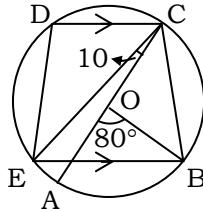
a. In the given figure, AC is diameter CD & BE are parallel. $\angle AOB = 80^\circ$, $\angle ACE = 10^\circ$.

Calculate:

i) $\angle BEC$

ii) $\angle BCD$

iii) $\angle CED$



[3]

Solution:

Statement

1) $\angle AOB + \angle BOC = 180^\circ$

2) $80^\circ + \angle BOC = 180^\circ$

3) $\angle BEC = \frac{1}{2} \angle BOC$

$\square \angle BEC = \frac{1}{2} \times 100^\circ = 50^\circ$

4) $\angle DCE = \angle BEC$

$\therefore \angle DCE = 50^\circ$

5) $\angle ACB = \frac{1}{2} \angle AOB$

Reason

Linear pair

Substitution.

$\angle BOC = 100^\circ$

Central \square s is twice the angle at remaining circumference.

alternate \square s.

Central \square s is twice are angle at remaining circumference.

$$\angle ACB = \frac{1}{2} \times 80^\circ = 40^\circ$$

$$6) \angle BCD = \angle DCE + \angle ACE + \angle ACB \quad \text{Angle addition Prop.}$$

$$\angle BCD = 50^\circ + 10^\circ + 40^\circ$$

$$\boxed{\angle BCD = 100^\circ}$$

$$7) \angle BCD + \angle BED = 180^\circ \quad \text{Opp } \square \text{s of angle } \square \text{ are suppl.}$$

$$8) \angle BCD + \angle BEC + \angle CED = 180^\circ \quad \text{Angle add P.}$$

$$100^\circ + 50^\circ + \angle CED = 180^\circ \quad \text{From 3 \& 6.}$$

$$\boxed{\angle CED = 30^\circ}$$

- b. The ratio of base area and curved surface area of a conical tent is 40: 41. If its height is 18 m. Find the air capacity of tent in terms of π . [3]

Solution:

For conical tent:

$$\text{Height (h) = 18 m}$$

According to given condition,

$$\frac{\text{Area of base}}{\text{Curved surface area}} = \frac{40}{41}$$

$$\frac{\pi r^2}{\pi r l} = \frac{40}{41}$$

$$r : l = 40 : 41$$

Let the common multiple be x.

$$\text{radius (r) = } 40x;$$

$$\text{slant height (l) = } 41x$$

$$l^2 = h^2 + r^2$$

... Pythagoras theorem

$$(41x)^2 = (18)^2 + (40x)^2$$

$$1681x^2 = 324 + 1600x^2$$

$$\therefore 1681x^2 - 1600x^2 = 324$$

$$81x^2 = 324$$

$$x^2 = \frac{324}{81} = 4$$

... Taking square root on both sides

$$x = 2$$

$$r = 40x = 40 \times 2 = 80 \text{ cm}$$

Air capacity of tent = Volume of cone

$$= \frac{1}{3} \pi r^2 h$$

$$= \frac{1}{3} \pi (80)^2 \times 18$$

$$\therefore \text{Air capacity of tent} = \underline{38400 \text{ m}^3}$$

- c. Mr. Batliwala has a R.D. Account of Rs. 300 per month. If the rate of interest is 12% & the maturity value is Rs. 8100. Find the time (in yrs.) of this R.D. Account. [4]

Solution:

Monthly Installment = ` 300

Let No. of months be 'n'.

Equivalent Principal for 1 month

$$(P) = MI \times \frac{n(n+1)}{2}$$

$$= 300 \times \frac{n(n+1)}{2}$$

$$\therefore P = 150 n(n+1)$$

Rate (R) = 12% p.a.

Time (T) = $\frac{1}{12}$ yr.

$$I = \frac{P \times R \times T}{100}$$

$$= \frac{150n(n+1) \times 12 \times 1}{100 \times 12}$$

$$I = \frac{5n(n+1)}{10}$$

$$\text{Actual deposit} = MI \times n$$

$$= 300 \times n$$

$$= `300n$$

$$\text{Maturity Value} = \left(\begin{array}{c} \text{Actual} \\ \text{deposit} \end{array} \right) + \text{Interest}$$

$$\therefore 8100 = 300n + \frac{15n(n+1)}{10}$$

$$8100 = \frac{600n + 3n^2 + 3n}{2}$$

$$\therefore 3n^2 + 603n = 16200$$

Divide each term by 3, we get,

$$n^2 + 201n - 5400 = 0$$

$$n^2 + 225n - 24n - 5400 = 0$$

$$n(n + 225) - 24(n + 225) = 0$$

$$(n + 225)(n - 24) = 0$$

... (Factorizing left side)

$$n + 225 - 0 = 0$$

$$\text{or } n - 24 = 0$$

... (Zero product rule)

$$n = -225$$

$$\text{or } n = 24$$

'n' cannot be negative

$$\therefore n = 24 \text{ months}$$

$$\therefore \text{Time} = \frac{24}{12} = 2 \text{ yrs.}$$

Question 7

- a. Show that $2x + 7$ is a factor of $2x^3 + 5x^2 - 11x - 14$. Hence factorize the given expression completely, using factor theorem. [3]

Solution:

$$f(x) = 2x^3 + 5x^2 - 11x - 14$$

By remainder theorem, when $f(x)$ is divided by $(2x + 7)$,

the remainder is $f\left(-\frac{7}{2}\right)$

$$f\left(-\frac{7}{2}\right) = 2\left(-\frac{7}{2}\right)^3 + 5\left(-\frac{7}{2}\right)^2 - 11\left(-\frac{7}{2}\right) - 14$$

$$f\left(-\frac{7}{2}\right) = 2\left(\frac{-343}{8}\right) + 5\left(\frac{49}{4}\right) + \frac{77}{2} - \frac{14}{1}$$

$$f\left(-\frac{7}{2}\right) = -\frac{343}{4} + \frac{245}{4} + \frac{77}{2} - \frac{14}{1}$$

$$f\left(-\frac{7}{2}\right) = \frac{-343 + 245 + 154 - 56}{4}$$

$$f\left(-\frac{7}{2}\right) = \frac{-399 + 399}{4}$$

$$f\left(-\frac{7}{2}\right) = \frac{0}{4} = 0$$

By factor theorem, $\therefore f\left(-\frac{7}{2}\right) = 0$

$(2x + 7)$ is a factor of $f(x)$.

For other factors:

$$\begin{array}{r}
 \begin{array}{r}
 2x + 7 \overline{) \begin{array}{l}
 x^2 - x - 2 \\
 2x^3 + 5x^2 - 11x - 14 \\
 - 2x^3 + 7x^2 \\
 \hline
 (-) \quad (-) \\
 -2x^2 - 11x - 14 \\
 - \quad -2x^2 - 7x \\
 \hline
 (+) \quad (+) \\
 -4x - 14 \\
 - \quad -4x - 14 \\
 \hline
 (+) \quad (+) \\
 \hline
 x
 \end{array}
 \end{array}
 \end{array}$$

$$f(x) = 2x^3 + 5x^2 - 11x - 14$$

$$f(x) = (2x + 7)(x^2 - x - 2)$$

$$= (2x + 7)(x^2 - 2x + x - 2)$$

$$= (2x + 7)[x(x - 2) + 1(x - 2)]$$

$$\therefore f(x) = (2x + 7)(x - 2)(x + 1)$$

b. Prove that: $(\sin A + \operatorname{cosec} A)^2 + (\cos A + \sec A)^2 = 7 + \tan^2 A + \cot^2 A$.

[3]

Solution:

$$\text{L.H.S.} = (\sin A + \operatorname{cosec} A)^2 + (\cos A + \sec A)^2$$

$$= \sin^2 A + 2 \sin A \cdot \operatorname{cosec} A + \operatorname{cosec}^2 A + \cos^2 A + 2 \cos A \cdot \sec A + \sec^2 A$$

$$\dots (a + b)^2 = a^2 + 2ab + b^2$$

$$= \sin^2 A + \operatorname{cosec}^2 A + 2 + \cos^2 A + 2 + \sec^2 A$$

$$\dots \sin \theta \times \operatorname{cosec} \theta = 1 \text{ \& } \sec \theta \times \cos \theta = 1$$

$$= 1 + \operatorname{cosec}^2 A + 2 + 2 + \sec^2 A \dots \sin^2 \theta + \cos^2 \theta = 1$$

$$= 5 + 1 + \cot^2 A + 1 + \tan^2 A$$

$$\dots \operatorname{cosec}^2 \theta = 1 + \cot^2 \theta \text{ \& } \sec^2 \theta = 1 + \tan^2 \theta$$

$$= 7 + \tan^2 A + \cot^2 A$$

$$\therefore \text{L.H.S.} = \text{R.H.S.}$$

... hence proved.

c. If $A = \begin{bmatrix} a & 0 \\ 0 & 2 \end{bmatrix}$, $B = \begin{bmatrix} 0 & -b \\ 1 & 0 \end{bmatrix}$, $M = \begin{bmatrix} 1 & -1 \\ 1 & 1 \end{bmatrix}$ & $BA = M^2$, find values of a & b.

[4]

Solution:

$$BA = M^2 \quad \dots \text{ given}$$

$$BA = M \cdot M$$

$$\begin{bmatrix} 0 & -b \\ 1 & 0 \end{bmatrix} \begin{bmatrix} a & 0 \\ 0 & 2 \end{bmatrix} = \begin{bmatrix} 1 & -1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & -1 \\ 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 0(a) + b(0) & 0(0) + b(2) \\ 1(a) + 0(0) & 1(0) + 0(2) \end{bmatrix} = \begin{bmatrix} 1(1) + (-1)1 & 1(-1) + (-1)1 \\ 1(1) + (1)(1) & 1(-1) + 1(1) \end{bmatrix}$$

$$\begin{bmatrix} 0 & -2b \\ a & 0 \end{bmatrix} = \begin{bmatrix} 0 & -2 \\ 2 & 0 \end{bmatrix}$$

Since the matrices are equal, their corresponding elements are also equal.

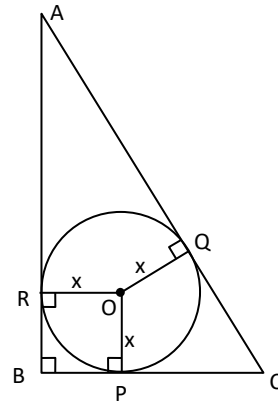
$$-2b = -2 \quad \& \quad a = 2$$

$$\therefore b = 1$$

$$\text{Ans.: } a = 2, b = 1$$

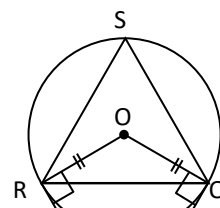
Question 8

- a **ABC is a right angled triangle. AB = 12 cm, AC = 13 cm. A circle with centre O has been inscribed inside the triangle. Calculate the value of x, the radius of inscribed circle. [3]**



Solution:

Statement	Reason
1) $OP = OR = OQ = x$... Radii of same circle
2) $\square OPBR$ is a square	... \because Each Angle is 90° & Adjacent sides are equal
3) $\therefore OP = BP = BR = x$... from (1)&(2)
4) In right $\triangle ABC$,	... Pythagoras theorem
$(AC)^2 = (AB)^2 + (BC)^2$... Substitution
$(13)^2 = (12)^2 + (BC)^2$	
$(BC)^2 = 169 - 144$	
$BC^2 = 25$... Taking square root on both sides
$BC = \underline{5 \text{ cm}}$	
5) $AR = AQ$... Tangents from ext. point are equal
6) $AQ = AB - BR$... $A-R-B$
$AQ = \underline{(12 - x)}$... from 3 & given
7) $CP = CQ$... Tangents from exterior point are equal
8) $CQ = BC - BP$... $B-P-C$
$CQ = \underline{(5 - x)}$	
9) $AC = AB + QC$... $A-Q-C$
$13 = 12 - x + 5 - x$... from (6)& (8)
$13 = 17 - 2x$	
$2x = 4$	
$x = \underline{2 \text{ cm}}$	
Radius = $x = \underline{2 \text{ cm}}$	



- b. The diameter of a sphere is 6 cm. It is melted & drawn into a wire of diameter 0.2 cm. Find the length of the wire.

Solution:

For sphere:

$$\text{Diameter} = 6 \text{ cm}$$

$$\text{Radius } (r_s) = \frac{6}{2} = 3 \text{ cm}$$

For cylindrical wire:

$$\text{Diameter} = 0.2 \text{ cm}$$

$$\text{Radius} = \frac{0.2}{2} = \underline{0.1 \text{ cm}}$$

$$\text{Length} = \text{Height} = ?$$

According to given condition,

$$\frac{4}{3} \pi r_s^3 = \pi r^2 h$$

$$\therefore \frac{4}{3} \times (3)^2 = (0.1)^2 \times h$$

$$h = \frac{4 \times 9}{0.1 \times 0.1} = \frac{36}{0.01} = 3600 \text{ cm} = 36 \text{ m}$$

$$\therefore \text{Length of wire} = \underline{36 \text{ m}}$$

- c. Mr. Ram Gopal invested ₹ 8000 in 7% ₹ 80. After a year he sold these shares at ₹ 75 each & invested the proceeding (including his dividend) in 18% ₹ 25 shares at ₹ 41. Find:
- Dividend for first year
 - Annual income in second year
 - Percentage increases in his return on his original investment.

[4]

Solution:

For first year:

$$\text{Investment} = ₹ 8000$$

$$\text{Face Value (FV)} = ₹ 100$$

$$\text{Market Value (MV)} = ₹ 80$$

$$\text{Rate of dividend} = 7\%$$

$$\begin{aligned} \text{i) No. of shares} &= \frac{\text{Investment}}{\text{MV}} \\ &= \frac{8000}{80} \\ &= 100 \text{ shares} \end{aligned}$$

$$\begin{aligned} \text{Dividend} &= \left(\frac{\text{Rate of dividend}}{100} \right) \times \text{FV} \times \left(\text{No. of Shares} \right) \\ &= \frac{7}{100} \times 100 \times 100 \end{aligned}$$

$$\text{Dividend} = \text{₹} 700 \text{ -----}$$

1m

For Second Year:

$$\text{SP of 1 share} = \text{₹} 75$$

$$\text{SP of 100 shares} = \text{₹} 7500$$

$$\text{Sale Proceeds} = \text{₹} 7500$$

$$\begin{aligned} \text{Investment} &= \text{Sale Proceed} + \text{Dividend} \\ &= 7500 + 700 \\ &= \text{₹} 8200 \text{ ----- 1m} \end{aligned}$$

$$\text{Face Value (FV)} = \text{₹} 25$$

$$\text{Market Value (MV)} = \text{₹} 41$$

$$\text{Rate of dividend} = 18\%$$

$$\begin{aligned} \text{ii) No. of shares} &= \frac{\text{Investment}}{\text{MV}} \\ &= \frac{8200}{41} = 200 \end{aligned}$$

$$\begin{aligned} \text{Dividend} &= \left(\frac{\text{Rate of dividend}}{100} \right) \times \text{FV} \times \left(\text{No. of Shares} \right) \\ &= \frac{18}{100} \times 25 \times 200 \end{aligned}$$

$$\text{Dividend} = \text{₹} 900 \text{ -----1m}$$

iii) Increase in Income

$$= \left(\text{Dividend in 2}^{\text{nd}} \text{ year} \right) - \left(\text{Divide in 1}^{\text{st}} \text{ year} \right)$$

$$\begin{aligned} &= 900 - 700 \\ &= \text{₹} 200 \end{aligned}$$

$$\begin{aligned} \text{Percentage Increase} &= \frac{\text{Increase}}{\text{Original Inv.}} \times 100 \\ &= \frac{200}{8000} \times 100 \end{aligned}$$

$$\text{Percentage Increase} = 2.5 \% \text{ -----1m}$$

Question 9

- a. During every financial year, the value of a machine depreciates by 12%. Find the original cost of a machine which depreciates by Rs.2640 during second financial year of its purchase. [3]

Solution:

For 1st year:

$$\text{Principal (P)} = \text{₹} P \quad \dots \text{ (assumption)}$$

$$\text{Rate (R)} = 12\% \text{ p.a.}$$

$$\text{Time (T)} = 1 \text{ year}$$

$$I = \frac{P \times R \times T}{100}$$

$$= \frac{P \times 12 \times 1}{100}$$

$$I = \frac{12P}{100}$$

$$A = P + I \quad \dots (\because \text{depreciation})$$

$$A = P - \frac{12P}{100} = \frac{88P}{100}$$

For 2nd year:

$$P = \frac{88P}{100}$$

$$R = 12\% \text{ p.a.}$$

$$T = 1 \text{ year}$$

$$I = \frac{P \times R \times T}{100}$$

$$2640 = \frac{88P \times 12 \times 1}{100 \times 100}$$

$$\therefore P = \frac{2640 \times 100 \times 100}{88 \times 12}$$

$$\therefore P = \text{` } 2500$$

Ans.: The original cost of a machine
= ` 25000.

- b. A open cylindrical vessel of internal diameter 7 cm & height 8 cm stands on a table. Inside this is place a solid metallic right circular cone, the diameter of whose base is $3\frac{1}{2}$ cm & height = 8 cm. Find volume of water required to fill the vessel. [3]**

Solution:

For cylindrical vessel,

$$\text{Diameter} = 7 \text{ cm}$$

$$\text{Radius (r)} = \frac{7}{2} \text{ cm}$$

$$\text{Height (h)} = 8 \text{ cm}$$

For solid metallic cone,

$$\text{Diameter} = \frac{7}{2} \text{ cm}$$

$$\text{Radius (r}_c) = \frac{7}{4} \text{ cm}$$

$$\text{Height (h)} = 8 \text{ cm} \quad \dots \text{ same as cylindrical vessel}$$

According to given condition,

$$\left(\begin{array}{l} \text{Volume of water} \\ \text{to fill the vessel} \end{array} \right) = \left(\begin{array}{l} \text{volume of} \\ \text{cylindrical vessel} \end{array} \right) - \left(\begin{array}{l} \text{Volume of} \\ \text{solid cone} \end{array} \right)$$

$$\begin{aligned}
&= \pi r^2 h - \frac{1}{3} \pi r_c^2 h \\
&= \pi h \left[r^2 - \frac{1}{3} r_c^2 \right] \\
&= \frac{22}{7} \times 8 \left[\left(\frac{7}{2} \right)^2 - \frac{1}{3} \times \left(\frac{7}{4} \right)^2 \right] \\
&= \frac{22}{7} \times 8 \left[\frac{49}{4} - \left(\frac{1}{3} \times \frac{49}{16} \right) \right] \\
&= \left[\frac{49}{4} - \frac{49}{48} \right] \\
&= \left[\frac{588 - 49}{48} \right] \\
&= \frac{22}{7} \times 8 \times \frac{539}{48} \\
&= \frac{847}{3} = 282.33
\end{aligned}$$

Volume of water = 282.33 cm³

c. A rectangular tank has length = 4 cm, width = 3 m & capacity = 30 m³. A small model of tank is made with capacity 240 cm³. Find:

i) Dimensions of model

ii) Ratio between total surface area of tank and its model.

[4]

Solution:

For rectangular tank,

Capacity = Vol. of cuboids

$$30 = l \times b \times h$$

$$\therefore h = \frac{30}{4 \times 3} = 2.5 \text{ cm}$$

$$* \frac{\text{Volume of model}}{\text{Volume of tank}} = k^3$$

$$\therefore \frac{240 \text{ cm}^3}{30 \text{ m}^3} = k^3$$

$$k^3 = \frac{240 \text{ cm}^3}{30 \times 100 \times 100 \times 100 \text{ cm}^3}$$

Taking cube root on both sides

$$k = \frac{2}{100}$$

$$k = \frac{1}{50}$$

$$i) \quad \frac{\text{length of model}}{\text{length of tank}} = k$$

$$\text{length of model} = \frac{1}{50} \times 4 \text{ m}$$

$$\text{length of model} = \frac{1}{50} \times 400 \text{ cm} = 8 \text{ cm}$$

$$\frac{\text{breadth of model}}{\text{breadth of tank}} = k$$

$$\therefore \text{breadth of model} = \frac{1}{50} \times 3 \text{ cm}$$

$$= \frac{1}{50} \times 300 \text{ cm}$$

$$\therefore \text{breadth of model} = 6 \text{ cm}$$

$$\frac{\text{Height of model}}{\text{Height of tank}} = k$$

$$\text{Height of model} = \frac{1}{50} \times 2.5 \text{ m}$$

$$= \frac{1}{50} \times 250 \text{ cm}$$

$$\text{Height of model} = 5 \text{ cm}$$

$$ii) \quad \frac{\text{Total surface area of model}}{\text{T.S.Area of tank}} = k^2$$

$$= \left(\frac{1}{50} \right)^2$$

$$= \frac{1}{2500}$$

$$\therefore \text{TSA of tank} : \text{TSA of model} = 2500 : 1$$

Question 10

a. Find the value of 'K' if $(x - 2)$ is a factor of $x^3 + 2x^2 - kx + 10$. Hence determine whether $(x + 5)$ is also a factor. [3]

Solution:

$$f(x) = x^3 + 2x^2 - kx + 10$$

By remainder theorem,

when $f(x)$ is divided by $(x - 2)$, the remainder is $f(2)$.

$$f(2) = (2)^3 + 2(2)^2 - k(2) + 10$$

$$= 8 + 8 - 2k + 10$$

$$f(2) = 26 - 2k \quad \dots (i)$$

$(x - 2)$ is a factor of $f(x)$... given

\therefore from (i) & (ii)

$$26 - 2k = 0$$

$$\therefore 2k = 26$$

$$\therefore k = 13$$

$$\therefore f(x) = x^3 + 2x^2 - 13x + 10$$

By remainder theorem, when $f(x)$ is divided by $(x + 5)$, the remainder is $f(-5)$.

$$\begin{aligned}\therefore f(-5) &= (-5)^3 + 2(-5)^2 - 13(-5) + 10 \\ &= -125 + 50 + 65 + 10 \\ &= -125 + 125\end{aligned}$$

$$f(-5) = 0$$

By factor theorem $\therefore f(-5) = 0$

$(x + 5)$ is a factor of $f(x)$.

b. A manufacturer sells a washing machine to a wholesaler sells it to a trader at a profit of ` 1500 & trader in turn sells it to a consumer at a profit of ` 1800. If the rate of VAT is 8%, find:

(i) Amount of VAT received by State Government on sale of this machine from manufacturer & the wholesaler.

(ii) the amount the consumer pays for the machine.

[3]

Solution:

For manufacturer:

i) $SP = ` 15000$

Rate of VAT = 8%

Tax received from manufacturer

= 8% of 15000

$$= \frac{8}{100} \times 15000$$

= ` 1200

\therefore VAT received by govt. from manufacture = ` 1200.

For wholesaler:

Profit = ` 1200

Rate of VAT = 8%

Tax received from wholesaler

= 8% of 12000

$$= \frac{8}{100} \times 12000$$

= ` 96

\therefore VHT received by govt. from wholesaler = ` 96

ii) Total SP = 15000 + 1200 + 1800
= ` 18000

Rate of ST = 8%

Amt. paid = ?

$$\text{Amt. paid} = SP \left(1 + \frac{\text{Rate of ST}}{100} \right)$$

$$= 18000 \left(1 + \frac{8}{100} \right)$$

$$= 18000 \left(\frac{108}{100} \right)$$

∴ Amt. paid by customer = ` 19440

- c. The mean of following distribution is 62.8 and the sum of all frequencies is 50. Find the missing frequencies f_1 & f_2 . [4]

Class	0-20	20-40	40-60	60-80	80-100	100-120
Frequency	5	f_1	10	f_2	7	8

Solution:

Class	frequency		$f \times x$
	x	f	
0-20	10	5	50
20-40	30	f_1	$30f_1$
40-60	50	10	500
60-80	70	f_2	$70f_2$
80-100	90	7	630
100-120	110	+ 8	+ 880
		$\sum f = 30 + f_1 + f_2$	$\sum fx = 2060 + 30f_1 + 70f_2$

$$\text{Now, Mean} = \frac{\sum fx}{\sum f}$$

$$\therefore 62.8 = \frac{2060 + 30f_1 + 70f_2}{50}$$

$$62.8 \times 50 = 2060 + 30f_1 + 70f_2$$

$$3140 - 2060 = 30f_1 + 70f_2$$

$$\therefore 30f_1 + 70f_2 = 1080$$

$$\therefore 3f_1 + 7f_2 = 108 \quad \dots (i)$$

$$\text{Also, } 30 + f_1 + f_2 = 50$$

$$f_1 + f_2 = 20 \quad \dots (ii)$$

Multiplying equation (ii) by 3,

$$3f_1 + 3f_2 = 60$$

$$-3f_1 + 7f_2 = 108$$

$$\begin{array}{r} (-) \quad (-) \quad (-) \\ \hline \end{array}$$

$$-4f_2 = -48$$

$$\therefore f_2 = \frac{48}{4}$$

$$\therefore f_2 = 12$$

Substitute f_2 in equation (ii),

$$f_1 + f_2 = 20$$

$$f_1 + 12 = 20$$

$$f_1 = 20 - 12$$

$$f_1 = 8$$

Ans.: $f_1 = 8$; $f_2 = 12$
