

GREENLAWNS SCHOOL, WORLI
Terminal Examination 2017
MATHEMATICS

STD: X
Date: 26/09/2017

Marks: 80
Time: 2½hrs

Section A

(Attempt all questions of this section)

Question 1

- a. Monica has a C.D. Account in Union Bank of India & deposited ₹ 600 per month. If the maturity value of this account is ₹ 24930 & the rate of interest is 10% p.a. Find the time (in yrs.) for which the account was held. [3]
- b. Identical cards are marked 1 to 75. When a card is drawn at random, what is the probability that it is;
(i) a multiple of 11.
(ii) a perfect square.
(iii) a factor of 75. [3]
- c. If $(x - 3)$ is a factor of $2x^3 + 3x^2 + px + 15$
(i) Find the value of p
(ii) Hence Factorise the expression completely. [4]

Question 2

- a. Represent the solution set of the following inequation on the number line.

$$x + \frac{1}{5} < 1\frac{1}{3}x + \frac{8}{15} \leq \frac{x}{5} + 1\frac{2}{3}, \quad x \in \mathbb{R} \quad [3]$$

- b. Mean of the following set of distribution is 18,
Calculate the numerical value of x. [3]

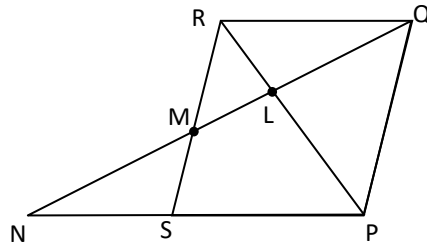
Marks	5	10	15	20	25	30
No. of Students	6	4	6	12	x	4

- c. The point P is the foot of perpendicular from A(-5, 7) to the line whose equation is $2x - 3y + 18 = 0$.
Determine: (i) The equation of the line AP.
(ii) The co-ordinates of P. [4]

Question 3.

- a. If $\begin{bmatrix} 3 & -24 \\ -1 & 4 \end{bmatrix} \begin{bmatrix} x \\ 2 \end{bmatrix} + 3 \begin{bmatrix} -4 \\ 5 \end{bmatrix} = 2 \begin{bmatrix} -3 \\ 9y \end{bmatrix}$, find x and y. [3]
- b. Prove that: $\frac{\cot A + \tan B}{\cot B + \tan A} = \cot A \tan B$. [3]

- c. In the figure, PQRS is a \parallel^m with PQ = 16cm, QR = 10cm. L is a point on PR such that RL : LP = 2 : 3 QL produced meets RS at M & PS produced at N. Find the lengths of PN & RM. [4]



Question 4

- a. Solve the quadratic equation and give your answer correct to two significant figures:
 $3x - 1 = \frac{7}{x}$ [3]
- b. Prove: $\sin^6\theta + \cos^6\theta = 1 - 3\sin^2\theta \cdot \cos^2\theta$ [3]
- c. Use graph paper for this question. A point P is reflected to P' in the Y-axis. The co-ordinates of its image are (-2, 3).
 (i) Find the co-ordinate of P.
 (ii) Find P'', the reflection of P under X-axis.
 (iii) Find the co-ordinates of Q' of Q(0, 2) after reflecting under PP".
 (iv) Write the special name of PP'QQ'.
 Also, find the area of the figure obtained. [4]

Section B (40 marks)

(Attempt any **Four** question from this Section)

Question 5

- a. Using properties of proportion, Solve for 'x'
 $\frac{x^2 + 3x - 4}{3x - 4} = \frac{3x^2 + 2x + 9}{2x + 9}$ [3]
- b. Find the value of 'K' if $(x - 2)$ is a factor of $x^3 + 2x^2 - kx + 10$. Hence determine whether $(x + 5)$ is also a factor. [3]
- c. The line joining P (-4, 5) & Q(3, 2) intersects y-axis at point R. PM & QN are perpendicular from P & Q on x-axis. Find:
 i) Ratio PR: RQ
 ii) Co-ordinates of R
 iii) Area of \square PMNQ [4]

Question 6

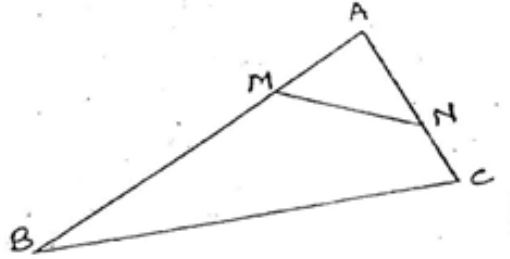
- a. If $\frac{x}{a} = \frac{y}{b} = \frac{z}{c}$; prove that $\frac{x^3}{a^2} + \frac{y^3}{b^2} + \frac{z^3}{c^2} = \frac{(x+y+z)^3}{(a+b+c)^2}$ [3]
- b. If $A = \begin{bmatrix} 1 & 0 \\ -1 & 7 \end{bmatrix}$ and $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ then find 'k' if $A^2 = 8A + kI$ [3]
- c. In what ratio is the line joining the points (4, 2) and (3, -5) divided by the x axis? Find the co-ordinates of the point of intersection. [4]

Question 7

- a. In $\triangle ABC$, M and N are points on AB and AC such that $AM = 2\text{cm}$, $MB = 4\text{cm}$, $AN = 3\text{cm}$ and $NC = 1\text{cm}$.

Prove that: $\triangle AMN \sim \triangle ACB$

Also, find $\frac{\text{Area of } \triangle AMN}{\text{Area of } \triangle ACB}$



[3]

- b. Ravina deposits ₹ 600 per month in a recurring deposit scheme for 2 years. If she receives ₹ 15,450 at the time of maturity, calculate the rate of interest per annum.

[3]

- c. Estimate the mode by drawing the histogram.

[4]

Class Interval	20 - 30	30 - 40	40 - 50	50 - 60	60 - 70	70 - 80
Frequency	10	6	8	12	5	9

Question 8

- a. If $(3x + 4) : (x + 5)$ is the duplicate ratio of $8 : 5$, find the value of x .

[3]

- b. Find the values of x , which satisfy the inequation:

$$-2 \leq \frac{1}{2} - \frac{2x}{3} \leq 1\frac{5}{6}, x \in \mathbb{N}.$$

Graph the solution on number line.

[3]

- c. A hemisphere is surmounted by a right circular cone of same base radius. If the common radius is 7 cm and slant height is 25 cm.

[4]

Find :

- the height of the cone,
- the volume of the solid,
- the total surface area of the solid.

Question 9

- a. A shopkeeper buys an article whose marked price is ₹ 40,000 from a Manufacturer at a discount of 10%. The rate of sales tax (under VAT) on the article is 5%. If he sells the article to a consumer at a discount of 5%, find:

- the VAT paid by the shopkeeper
- the amount paid by the consumer.

[3]

- b. Draw a circle of radius 4 cm. Construct two tangents to this circle so that the angle between the tangents is 45° .

[3]

- c. Sum of two natural numbers is 8 and the difference of their reciprocal is $\frac{2}{15}$. Find the number.

[4]

Question 10

- a. Show that the points (3, 3), (9, 0), (12, 21) are the vertices of a right angled triangle. [3]
- b. The Top of an unfinished dam subtends an angle of elevation at a point 100 m from its base of 30° . How much higher should the dam be raised so that the angle of elevation becomes 45° . [3]
- c. Jayant sold some 100 shares at ₹ 90 and invested in 15% 50 shares at ₹ 33. If he sold this shares at ₹ 110 instead of ₹ 90, he would have earned ₹ 450 more. Find the number of shares sold by him. [4]

Question 11

- a. Given: $\cos\theta + \sin\theta = \sqrt{2} \cos\theta$.
Show that: $\cos\theta - \sin\theta = \sqrt{2} \sin\theta$. [4]
- b. The results of an examination are tabulated below: [6]

Marks(less than)	10	20	30	40	50	60	70	80	90	100
No. of Candidates	8	20	40	75	125	160	188	192	197	200

Taking 2 cm. = 10 marks on one axis and 2 cm. = 20 students on the other, draw an ogive for the above data and from it determine:

- (i) The median marks.
- (ii) The lower quartile.
- (iii) The inter quartile.
- (iv) The number of candidates who failed if pass mark is 35.
- (v) The number of candidates who obtained grade A, if the lowest mark for grade A is 75.

ANSWER KEY
SECTION A

Question 1

a.

Solution: Monthly Installment = ` 600 ,Let No. of months be 'n'.
Equivalent Principal for 1 month

$$(P) = MI \times \frac{n(n+1)}{2}$$

$$= 600 \times \frac{n(n+1)}{2}$$

$$\therefore P = 300n(n+1)$$

$$\text{Rate (R)} = 10\% \text{ p.a.}$$

$$\text{Time (T)} = \frac{1}{12} \text{ yr.}$$

$$I = \frac{P \times R \times T}{100}$$

$$= \frac{300n(n+1) \times 10 \times 1}{100 \times 12}$$

$$I = \frac{5n(n+1)}{2}$$

$$\text{Actual deposit} = MI \times n$$

$$= ` 600n$$

$$\text{Maturity Value} = \left(\begin{array}{c} \text{Actual} \\ \text{deposit} \end{array} \right) + \text{Interest}$$

$$24930 = 600n + \frac{5n(n+1)}{2}$$

$$24930 = \frac{1200n + 5n^2 + 5n}{2}$$

$$\therefore 5n^2 + 1205n = 49860$$

$$\therefore 5n^2 + 1205n - 49860 = 0$$

Divide each term by 5, we get,

$$n^2 + 241n - 9972 = 0$$

$$n^2 + 277n - 36n - 9972 = 0$$

$$n(n + 277) - 36(n + 277) = 0$$

$$(n + 277)(n - 36) = 0 \quad \dots \text{(Factorizing left side)}$$

$$n + 277 - 0 = 0 \quad \text{or} \quad n - 36 = 0 \dots \text{(Zero product rule)}$$

$$n = -277 \quad \text{or} \quad n = 36$$

'n' cannot be negative

$$\therefore n = 36 \text{ months}$$

$$\therefore \text{Time} = \frac{36}{12} = 3 \text{ yrs.}$$

b. Total Number of outcomes = 73

(i) Favorable outcomes = {11, 22, 33, 44, 55, 66}

No. of favourable outcomes = 6

$$\text{Probability} = \frac{\text{No. of favourable outcomes}}{\text{Total number of outcomes}} = \frac{6}{75} = \frac{2}{25}$$

(ii) Favorable outcomes = {1, 2, 3, 4, 5, 6, 7, 8}

No. of favourable outcomes = 8

$$\text{Probability} = \frac{\text{No. of favourable outcomes}}{\text{Total number of outcomes}} = \frac{8}{75}$$

(iii) Favorable outcomes = {1, 3, 5, 15, 25, 75}

No. of favourable outcomes = 6

$$\text{Probability} = \frac{6}{75} = \frac{2}{25}$$

c. $f(x) = 2x^3 + 3x^2 + px + 15$
Given $x - 3 = 0 \Rightarrow x = 3$
By factor theorem $f(3) = 0$
 $2x^3 + 3x^2 + 3p + 15 = 0$
 $54 + 27 + 3p + 15 = 0 \Rightarrow 3p = -96$
 $p = \frac{-96}{3} = p = -32$
 $\therefore f(x) = 2x^3 + 3x^2 - 32x + 15$

$$\begin{array}{r} 2x^2 + 9x - 5 \\ x - 3 \overline{) 2x^3 + 3x^2 - 32x + 15} \\ \underline{2x^3 - 6x^2} \\ - 9x^2 - 32x + 15 \\ \underline{+ 27x} \\ -5x + 15 \\ \underline{-5x + 15} \\ \underline{+ -} \\ \underline{0} \end{array}$$

$$\begin{aligned} \therefore f(x) &= (x - 3)(2x^2 + 9x - 5) \\ &= (x - 3)(2x^2 - x + 10x - 5) \\ &= (x - 3)[x(2x - 1) + 5(2x - 1)] \\ &= (x - 3)(2x - 1)(x + 5) \end{aligned}$$

Q.2.

a. $x + \frac{1}{5} < 1\frac{1}{3}x + \frac{8}{15} \leq \frac{x}{5} + 1\frac{2}{3}, \quad x \in \mathbb{R}$

$$\frac{5x+1}{5} < \frac{4x}{3} + \frac{8}{15} \leq \frac{x}{5} + \frac{5}{5}$$

$$\frac{5x+1}{5} < \frac{20x+8}{15} \leq \frac{3x+25x}{15}$$

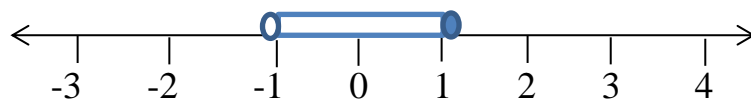
$$\frac{5x+1}{5} < \frac{20x+8}{15} \text{ and } \frac{20x+8}{15} \leq \frac{3x+25x}{15}$$

$$15x + 3 < 20x + 8 \text{ and } 17x \leq 17$$

$$-5 < 5x \quad \text{and} \quad x \leq 1$$

$$-1 < x$$

Solution set $\{x : -1 < x \leq 1 \mid x \in \mathbb{R}\}$



b. Mean = 18

x	f	fx
5	6	30
10	4	40
15	6	90
20	12	240
25	X	25x
30	4	120
	$32 + x$	$520 + 25x$

$$\text{Mean} = \frac{efx}{ef}$$

$$18 = \frac{520+25x}{32+x} \quad = \quad \frac{576 + 18x}{56} = \frac{52 + 25x}{7x}$$

$$x = 8$$

c. $2x - 3y + 18 = 0$ (i)

$$3y = 2x + 18$$

$$y = \frac{2}{3}x + 6$$

$$\text{Slope of AP} = \frac{-3}{2}$$

Equation of AP

$$y - y_1 = m(x - x_1)$$

$$y - 7 = \frac{-3}{2}[x - (-5)]$$

$$2y - 14 = -3x - 15$$

$$3x + 2y + 1 = 0$$

$$3x + 2y = -1 \quad \dots(i)$$

$$2x - 3y = -18 \quad \dots(ii)$$

Multiplying eg. (i) by 3 and (ii) by 2

$$9x + 6y = -3 \quad \dots(iii)$$

$$4x - 6y = -36 \quad \dots(iv)$$

Adding (i) & (ii)

$$13x = -39$$

$$x = -3$$

Substituting value of x in eg. (i)

$$3(-3) + 2y = -1$$

$$-9 + 2y = -1$$

$$2y = 8$$

$$y = 4$$

p(-3, 4)

Q.3.

$$a. \begin{bmatrix} 3 & -2 \\ -1 & 4 \end{bmatrix} \begin{bmatrix} 4x \\ 2 \end{bmatrix} + 3 \begin{bmatrix} -4 \\ 5 \end{bmatrix} = 2 \begin{bmatrix} -3 \\ 9y \end{bmatrix}$$

$$\begin{bmatrix} 3(4x) & -2(2) \\ -1(4x) & +4(2) \end{bmatrix} + \begin{bmatrix} -12 \\ 15 \end{bmatrix} = \begin{bmatrix} -6 \\ 18y \end{bmatrix}$$

$$\begin{bmatrix} 12x & -4 \\ -4x & +8 \end{bmatrix} + \begin{bmatrix} -12 \\ 15 \end{bmatrix} = \begin{bmatrix} -6 \\ 18y \end{bmatrix}$$

$$\begin{bmatrix} 12x & -4 + (-12) \\ -4x & +8 + 15 \end{bmatrix} = \begin{bmatrix} -6 \\ 18y \end{bmatrix}$$

$$\begin{bmatrix} 12x & -16 \\ -4x & +23 \end{bmatrix} = \begin{bmatrix} -6 \\ 18y \end{bmatrix}$$

Equating the matrices

$$12x - 16 = -6$$

$$12x = 10$$

$$x = \frac{10}{12}$$

$$x = \frac{5}{6}$$

$$-4x + 23 = 18y$$

$$-4\left(\frac{5}{6}\right) + 23 = 18y$$

$$\frac{-10}{3} + 23 = 18y$$

$$-10 + 69 = 54y$$

$$\frac{59}{54} = y$$

$$\frac{5}{54} = y$$

b. **Solution:**

$$\text{L.H.S.} = \frac{\cot A + \tan B}{\cot B + \tan A}$$

$$= \frac{\cot A + \tan B}{\frac{1}{\tan B} + \frac{1}{\cot A}}$$

$$\dots \tan \theta = \frac{1}{\cot \theta}, \cot \theta = \frac{1}{\tan \theta}$$

$$= (\cot A + \tan B) \div \left(\frac{\cot A + \tan B}{\cot A \cdot \tan B} \right)$$

$$= (\cot A + \tan B) \times \frac{\cot A \cdot \tan B}{(\cot A + \tan B)}$$

$$= \cot A \cdot \tan B$$

$$\therefore \text{L.H.S.} = \text{R.H.S.}$$

... hence proved.

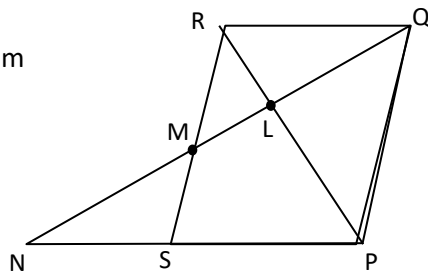
c. **Solution:**

□PQRS is a parallelogram

PQ = 16 cm

QR = 10 cm

RL : LP = 2 : 3



To find: PN, RM

Proof:

	Statement	Reason
1)	In $\triangle RQL$ & $\triangle PNL$, $\angle RQL = \angle PNL$ $\angle RLQ = \angle PLN$	Alternate angles are equal V.O.As
2)	$\triangle RQL \sim \triangle PNL$	By AA axiom of similarity
3)	$\frac{RQ}{PN} = \frac{RL}{PL}$	c.s.s.t.p.
4)	$\frac{10}{PN} = \frac{2}{3}$	Substitution

	$\therefore PN = \frac{10 \times 3}{2}$ $PN = 15 \text{ cm}$	Simplification
5)	In $\triangle RLM$ & $\triangle PLQ$, $\angle RLM = \angle PLQ$ $\angle LRM = \angle LPQ$	(V.O.As) alternate angles are equal
6)	$\triangle RLM \sim \triangle PLQ$	By AA axiom of similarity
7)	$\frac{RL}{PL} = \frac{RM}{PQ}$	c.s.s.t.p.
8)	$\frac{2}{3} = \frac{RM}{16}$	Substitution
9)	$RM = \frac{16 \times 2}{3}$ $RM = \frac{32}{3} = 10\frac{2}{3} \text{ cm}$	Simplification

m^2

Q.4.

a.

$$3x - 1 = \frac{7}{x}$$

$$3x^2 - x = 7$$

$$3x^2 - x - 7 = 0$$

$$a = 3 \quad b = -1 \quad c = -7$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-(-1) \pm \sqrt{(-1)^2 - 4 \times 3 \times (-7)}}{2 \times 3}$$

$$= +1 \pm \frac{1 + 85}{6} = \frac{1 \pm 9.22}{6}$$

$$x = \frac{1 + 9.22}{6} \quad \text{or} \quad x = \frac{1 - 9.22}{6}$$

$$= \frac{10.22}{6} \quad \text{or} \quad x = \frac{1(9.22 - 1)}{6}$$

$$= 1.703 \quad \text{or} \quad x = \frac{-8.22}{6} =$$

$$= 1.7 \quad \text{or} \quad x = -1.37 = x = -1.4$$

b. Prove: $\sin^6\theta + \cos^6\theta = 1 - 3\sin^2\theta \cdot \cos^2\theta$

$$\begin{aligned} \text{LHS} &= \sin^6\theta + \cos^6\theta \\ &= (\sin^2\theta)^3 + (\cos^2\theta)^3 \\ &= (\sin^2\theta + \cos^2\theta)(\sin^4\theta - \sin^2\theta\cos^2\theta + \cos^4\theta) \\ &= (\sin^2\theta + \cos^2\theta = 1) \\ &= \sin^4\theta - \sin^2\theta\cos^2\theta + \cos^4\theta \\ &= \sin^4\theta + \cos^2\theta - \sin^2\theta\cos^2\theta \\ &= (\sin^2\theta)^2 + (\cos^2\theta)^2 - \sin^2\theta\cos^2\theta \\ &= a^2 + b^2 = (a + b)^2 - 2ab \end{aligned}$$

$$\begin{aligned}
&= (\sin^2\theta + \cos^2\theta) - 2 \sin^2\theta \cos^2\theta - \sin^2\theta \cos^2\theta \\
&= 1 - 3\sin^2\theta \cos^2\theta \\
&= \text{RHS} \\
&\text{Hence Proved.}
\end{aligned}$$

- c.
- (i) $p(2, 3)$
 - (ii) $p''(2, -3)$
 - (iii) $9'(4, 2)$
 - (iv) Parallelogram
- Area $x = \frac{1}{2} \times 6 \times 4 +$
(graph paper)

Section B (40 marks)

Q.5.

a.
$$\frac{x^2 + 3x - 4}{3x - 4} = \frac{3x^2 + 2x + 9}{2x + 9}$$

Componendo & Dividendo

$$\frac{x^2 + 3x - 4 + 3x - 4}{x^2 + 3x - 4 - 3x + 4} = \frac{3x^2 + 2x + 9 + 2x + 9}{3x^2 + 2x + 9 - 2x - 9}$$

$$\frac{x^2 + 6x - 8}{x^2} = \frac{3x^2 + 4x + 18}{3x^2}$$

$$\frac{3x^2}{x^2} = \frac{3x^2 + 4x + 18}{x^2 + 6x - 8}$$

$$3x^2 + 18x - 24 = 3x^2 + 4x + 18$$

$$14x = 42$$

$$x = \frac{42}{14}$$

$$x = 3$$

b.

Solution:

$$f(x) = x^3 + 2x^2 - kx + 10$$

By remainder theorem,

when $f(x)$ is divided by $(x - 2)$, the remainder is $f(2)$.

$$f(2) = (2)^3 + 2(2)^2 - k(2) + 10$$

$$= 8 + 8 - 2k + 10$$

$$f(2) = 26 - 2k \quad \dots (i)$$

$(x - 2)$ is a factor of $f(x)$... given

\therefore from (i) & (ii)

$$26 - 2k = 0$$

$$\therefore 2k = 26$$

$$\therefore k = 13$$

$$\therefore f(x) = x^3 + 2x^2 - 13x + 10$$

By remainder theorem, when $f(x)$ is divided by $(x + 5)$, the remainder is $f(-5)$.

$$\therefore f(-5) = (-5)^3 + 2(-5)^2 - 13(-5) + 10$$

$$= -125 + 50 + 65 + 10$$

$$= -125 + 125$$

$$f(-5) = 0$$

By factor theorem $\therefore f(-5) = 0$

$(x + 5)$ is a factor of $f(x)$.

C. Solution:

$R(0, y)$ is point on y-axis

$P(-4, 5) \equiv (x_1, y_1)$ & $Q(3, 2) \equiv (x_2, y_2)$

By section formula,

$$R(0, y) = \left\{ \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right\}$$

$$R(0, y) = \left\{ \frac{m_1(3) + m_2(-4)}{m_1 + m_2}, \frac{m_1(2) + m_2(5)}{m_1 + m_2} \right\}$$

$$R(0, y) = \left\{ \frac{3m_1 - 4m_2}{m_1 + m_2}, \frac{2m_1 + 5m_2}{m_1 + m_2} \right\}$$

Equating x & y co-ordinates, we get,

$$0 = \frac{3m_1 - 4m_2}{m_1 + m_2} \quad \& \quad y = \frac{2m_1 + 5m_2}{m_1 + m_2}$$

$$\therefore 0 = 3m_1 - 4m_2 \quad \left| \quad y = \frac{2(4) + 5(3)}{4 + 3}$$

$$\therefore 3m_1 = 4m_2$$

$$y = \frac{8 + 15}{7}$$

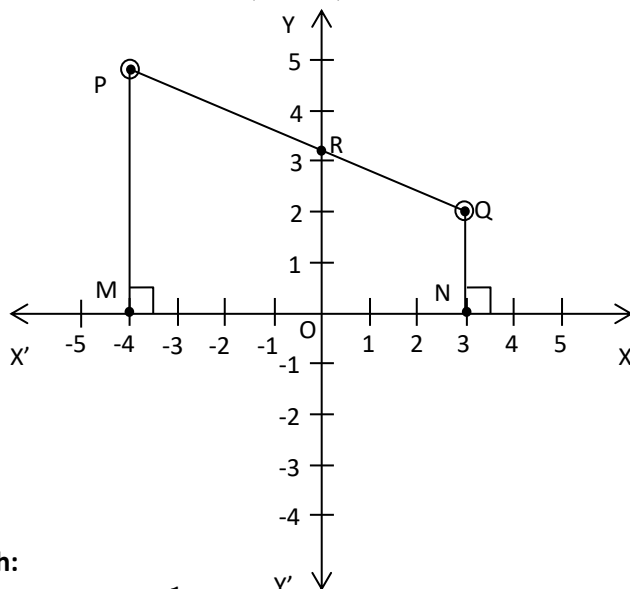
$$\frac{m_1}{m_2} = \frac{4}{3}$$

$$y = \frac{23}{7}$$

i) $PR : RQ = m_1 : m_2 = 4 : 3$

ii) Co-ordinates of $R(0, y) = \left(0, \frac{23}{7}\right)$

iii)



For graph:

$$\text{Area } \square \text{ PMNQ} = \frac{1}{2} (\text{sum of sides}) \times h$$

$$= \frac{1}{2} (5 + 2) \times 7$$

$$= \frac{49}{2}$$

$$\text{Area } \square \text{ PMNQ} = \underline{24.5 \text{ sq. units}}$$

Q.6.

a. Let $\frac{x}{a} = \frac{y}{b} = \frac{z}{c} = k$

$$k = \frac{x}{a} = \frac{y}{b} = \frac{z}{c}$$

$$\text{To prove} = \frac{x^3}{a^2} + \frac{y^3}{b^2} + \frac{z^3}{c^2} = \frac{(x+y+z)^3}{(a+b+c)^2}$$

$$\text{LHS} = \frac{a^3 b^3 c^3}{a^2 b^2 c^2}$$

$$= k^3(a + b + c)$$

$$\text{RHS} = \frac{(ak+bk+ck)^3}{(a+b+c)^2}$$

$$= \frac{((k^3(a+b+c))^3}{(a+b+c)^2}$$

$$= \frac{k^3(a+b+c)^3}{(a+b+c)^2}$$

$$= k^3(a + b + c)$$

$$= \text{LHS} \quad \text{Hence proved}$$

b. $A = \begin{bmatrix} 1 & 0 \\ -1 & 7 \end{bmatrix}$ $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

$$A^2 = 8A + kI$$

According to the given condition:

$$A^2 = 8A + KI$$

$$A^2 - 8A = KI$$

$$\begin{bmatrix} 1 & 0 \\ -1 & 7 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} - 8 \begin{bmatrix} 1 & 0 \\ -1 & 7 \end{bmatrix} = k \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 \\ -8 & 49 \end{bmatrix} - \begin{bmatrix} 8 & 0 \\ 8 & 56 \end{bmatrix} = \begin{bmatrix} k & 0 \\ 0 & k \end{bmatrix}$$

$$\begin{bmatrix} 1-8 & 0 \\ -8+8 & 49-56 \end{bmatrix} = \begin{bmatrix} k & 0 \\ 0 & k \end{bmatrix}$$

$$\begin{bmatrix} -7 & 0 \\ 0 & -7 \end{bmatrix} = \begin{bmatrix} k & 0 \\ 0 & k \end{bmatrix}$$

By equality of matrices corresponding values are equal

$$\therefore k = -7$$

c. Let $A = (4, 2)$

Let B = (3, -5)

Let k on x-axis

By section formulas

(x, 0) =

Q.7.

a. In $\triangle AMN$ and $\triangle ACB$

$\angle A = \angle A$ (common angle)

$$\frac{AM}{AC} = \frac{AN}{AB} = \frac{1}{2}$$

$\therefore \triangle AMN \sim \triangle ACB$

$$\frac{\text{Area of } \triangle AMN}{\text{Area of } \triangle ACB} = \left(\frac{AM}{AC} \right)^2$$

$$= \left(\frac{2}{4} \right)^2$$

$$= \left(\frac{1}{2} \right)^2$$

$$\frac{\text{Area of } \triangle AMN}{\text{Area of } \triangle ACB} = \frac{1}{4}$$

b. P = ` 600

N = 24 months

MV = ` 15,450

R = ?

$$MV = p \times n + p \times \frac{n(n+1)}{100} \times \frac{1}{12 \times 2}$$

$$15450 = 600 \times 24 + \frac{600 \times 24 \times 25 \times r}{100 \times 12 \times 2}$$

$$15450 = 14400 + 25 \times r$$

$$15450 = 150r$$

$$r = 7\%$$

c. (graph paper)

Q.8.

a. $\frac{3x+4}{x+5} = \left(\frac{8}{5}\right)^2$

$$\frac{3x+4}{x+5} = \frac{64}{25}$$

$$75x + 100 = 64x + 320$$

$$11x = 220$$

$$x = 20$$

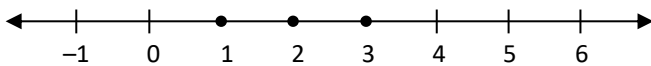
b. **Solution:**

$$\begin{array}{l} -2 \leq \frac{1}{2} \times 6 - \frac{2x}{3} \times 6 \\ -12 \leq 3 - 4x \\ \therefore 4x \leq 3 + 12 \\ \therefore 4x \leq 15 \\ \therefore x \leq \frac{15}{4} \\ \therefore x \leq 3.75 \end{array} \quad \& \quad \begin{array}{l} \frac{1}{2} \times 6 - \frac{2x}{3} \times 6 \leq \frac{11 \times 6}{6} \\ 3 - 4x \leq 11 \\ 3 - 11 \leq 4x \\ \therefore -8 \leq 4x \\ \text{i.e. } 4x \geq -8 \\ x \geq -\frac{8}{4} \\ \therefore x \geq -2 \end{array}$$

$$\therefore -2 \leq x \leq 3.75, x \in \mathbb{N}$$

$$\therefore \text{S.S.} = \{1, 2, 3\}$$

The graph of the solution is:



c. (i) $l^2 = h^2 + v^2$

$$(25)^2 = h^2 + (7)^2$$

$$625 = h^2 + 49$$

$$h^2 = 576$$

$$h = 24 \text{ cm}$$

(ii) Volume of the solid = v of conc + v of hemisphere

$$= \frac{1}{3} \pi r^2 h + \frac{2}{3} \pi r^3$$

$$= \frac{1}{3} \pi r^2 (h + 2r)$$

$$= \frac{1}{3} \times \frac{22}{7} \times 7 \times 7 (24 + 2(7))$$

$$= \frac{1}{3} \times 22 \times 7 \times 38$$

$$= \frac{5852}{3}$$

$$= 1950.666 \text{ cm}^2$$

$$= 1950.67 \text{ cm}^2$$

(iii) SA of solid = CSA of conc + CSA of hemisphere

$$= \pi r (l + 2r)$$

$$= \frac{22}{7} \times 7 (25 + 2 \times 7)$$

$$= 22 \times 39 = 858 \text{ cm}^2$$

Q.9.

a. MP = ₹ 40,000 /-

For shopkeeper

$$\begin{aligned} \text{Purchased price} &= 40,000 - \frac{1}{100} \times 40,000 \\ &= 40,000 - 4000 \\ &= 36,000 \end{aligned}$$

$$\begin{aligned} \text{Tax paid} &= \frac{5}{100} \times 36000 \\ &= ₹ 1800 \end{aligned}$$

$$\begin{aligned} \text{Selling price} &= 40,000 - \frac{5}{100} \times 40,000 \\ &= 40,000 - 2000 \\ &= 38,000 \end{aligned}$$

$$\begin{aligned} \text{Tax changed} &= \frac{5}{100} \times 38,000 \\ &= 1900 \end{aligned}$$

$$\begin{aligned} \text{VAT} &= \text{Tax changed} - \text{Tax paid} \\ &= 1900 - 1800 \\ &= ₹ 100 \end{aligned}$$

$$\begin{aligned} \text{Amt paid by customer} &= 38000 + 1900 \\ &= 39,900/- \end{aligned}$$

Q.9.

b. Construction

Q.9.

c. let two natural numbers be x and $8-x$

$$\frac{1}{x} - \frac{1}{8-x} = \frac{2}{15}$$

$$\frac{9-x-x}{x(8-x)} = \frac{2}{15}$$

$$\frac{8-2x}{8x-x^2} = \frac{2}{15}$$

$$\begin{aligned} 120 - 30x &= 16x - 2x^2 \\ 2x^2 - 16x - 30x + 120 &= 0 \\ 2x^2 - 46x + 120 &= 0 \\ 2x^2 - 23x + 60 &= 0 \end{aligned}$$

$$\begin{aligned}
x^2 - 20x + 3x + 60 &= 0 \\
x(x-20) - 3(x-20) &= 0 \\
(x-20)(x-3) &= 0 \\
x-20 = 0 \text{ or } x-3 &= 0 \\
x = 0 \text{ or } x = 3
\end{aligned}$$

But $x = 20$ is not possible

$$\therefore x = 3$$

$$\therefore 8 - x = 8 - 3 = 5$$

Thus the two numbers are 3 and 5.

Q.10.

a. Distance Formula for (3, 3) and (9, 0)

$$= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(3 - 9)^2 + (3 - 0)^2}$$

$$= \sqrt{36 + 9}$$

$$= \sqrt{45}$$

Distance Formula for (3, 3) and (12, 21)

$$= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(3 - 12)^2 + (3 - 21)^2}$$

$$= \sqrt{81 + 324}$$

$$= \sqrt{405}$$

Distance Formula for (3, 3) and (12, 21)

$$= \sqrt{(12 - 9)^2 + (21 - 0)^2}$$

$$= \sqrt{9 + 441}$$

$$= \sqrt{450}$$

$$\therefore (\sqrt{405})^2 + (\sqrt{45})^2 = (\sqrt{450})^2$$

$$405 + 45 = 450$$

$$450 = 450$$

\therefore By Pythagoras Theorem

(9, 0), (3, 3) and (12, 21) are the vertices of a right angled triangle.

b.

c. let the number of shares be x

Case I :

$$\begin{aligned}\therefore \text{Investment} &= 90 \times x \\ &= 90x\end{aligned}$$

$$\begin{aligned}\therefore \text{No of shares} &= \frac{\text{Investment}}{\text{market value}} \\ &= \frac{90x}{33} = \frac{30x}{11}\end{aligned}$$

$$\begin{aligned}\therefore \text{Income} &= \text{No. of shares} \times \text{Rate} \times \text{NV} \\ &= \frac{30x}{11} \times \frac{15}{11} \times 50 \\ &= \frac{225x}{11}\end{aligned}$$

Case II

$$\begin{aligned}\text{Investment} &= 110 \times x \\ &= 110x\end{aligned}$$

$$\therefore \text{No of shares} = \frac{110x}{33} = \frac{10x}{3}$$

$$\begin{aligned}\therefore \text{Income} &= \text{No. of shares} \times \text{NV} \times \text{Rate} \\ &= \frac{10x}{3} \times 50 \times \frac{15}{100} \\ &= \frac{75x}{3} \\ &= 25x\end{aligned}$$

According to condition

$$25x - \frac{225x}{11} = 450$$

$$\frac{275x - 225x}{11} = 450$$

$$50x = 450 \times 11$$

$$x = \frac{450 \times 11}{50}$$

$$x = 99 \text{ shares}$$

Q.11.

$$\begin{aligned}\text{a. } \cos \theta + \sin \theta &= \sqrt{2} \cos \theta \\ \sin \theta &= \sqrt{2} \cos \theta - \cos \theta\end{aligned}$$

$$= \cos \theta (\sqrt{2} - 1)$$

$$\frac{\sin \theta}{\cos \theta} = \sqrt{2} - 1$$

$$\frac{\cos \theta}{\sin \theta} = \frac{1}{\sqrt{2} - 1}$$

$$\frac{\cos \theta}{\sin \theta} = \frac{\sqrt{2} + 1}{(\sqrt{2})^2 - 1}$$

$$= \sqrt{2} + 1$$
$$\cos \theta = \sqrt{2} \sin \theta + \sin \theta$$
$$\cos \theta - \sin \theta = \sqrt{2} \sin \theta$$

b. Graph