

GREENLAWNS HIGH SCHOOL
TERMINAL EXAMINATION YEAR 2019

SUBJECT : MATHEMATICS

CLASS : X

TIME : 2 ½ HOURS

MARKS: 80

You will not be allowed to write during the first 10 minutes. This time is to be used in reading the question paper. Attempt all questions from section A and any four questions from Section B.

All working including rough work must be done on the same sheet as the rest of the answer.

Section A (40 Marks)

(Attempt all questions from this section)

I

- a. Solve the following inequation and graph the solution on a number line. (3)

$$-2\frac{1}{6} \leq \frac{x}{3} - 1\frac{1}{6} < \frac{5}{6}, x \in \mathbb{N}$$

- b. Find matrix Z if (3)

$$\begin{bmatrix} 3 & 2 \\ 5 & -4 \end{bmatrix} + Z = \begin{bmatrix} 8 & -2 \\ 7 & 9 \end{bmatrix} - \begin{bmatrix} 6 & -3 \\ 3 & 8 \end{bmatrix}$$

- c. The line $3y = 4x + 18$ intersects the Y-axis at A. Find (i) co-ordinates of A (4)
(ii) Equation of the line through A and parallel to the line $3x + 2y = 6$

II

- a. A person deposits a certain sum of money every month in a recurring deposit (3)
Account for 2 years. If he receives Rs. 71,550 on maturity at 10% p.a. Calculate
the monthly installment.

- b. Prove that $\frac{\cot^2 A}{(\operatorname{cosec} A + 1)^2} = \frac{1 - \sin A}{1 + \sin A}$ (3)

- c. Find 'a' if the mean of the following distribution is 33.68 (4)

C.I.	10 - 18	18 - 26	26 - 34	34 - 42	42 - 50
f	4	7	a	18	10

III

- a. Using the properties of proportion solve for x (3)

$$\frac{x^3 + 12x}{6x^2 + 8} = \frac{682}{182}$$

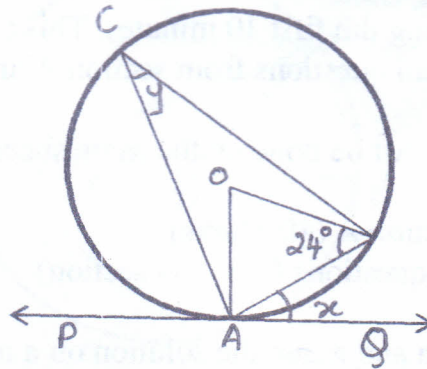
- b. Find the value of 'p' if the roots of the following equation are real and equal. (3)

$$(p + 1)x^2 - 2(3p + 1)x + 8p + 1 = 0$$

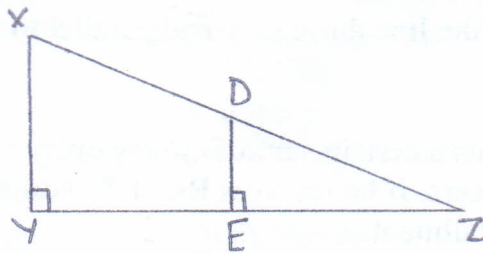
- c. Using factor theorem show that $(x - 1)$ is a factor of $x^3 - 7x^2 + 14x - 8$. (4)
Hence mention all the factors of the given expression.

IV .

- a. In the figure drawn below, O is the centre of the circle. Find x and y if PQ is a tangent to the circle at A. (3)



- b. In the figure drawn below XY and DE are perpendiculars to YZ. If $XY = 12$ cm, $DE = 8$ cm, $XZ = 4x + 2$ and $DZ = 3x - 1$, find XD (3)

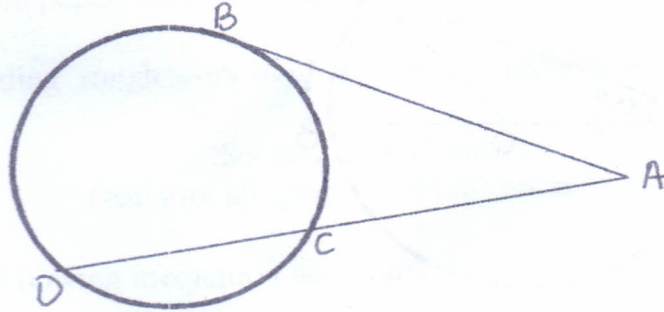


- c. Construct a regular hexagon whose each side measures 4.5 cm. Construct a circle touching the vertices of the hexagon and record its radius. (4)

Section B
(Any 4 out of 5)

V

- a. In the figure drawn below AB is a tangent to the circle at B. If $AB = 24$ cm, $CD = 20$ cm find AC (3)



- b. A right circular cone is 10.8 cm high and the radius of the base is 1.6 cm. It is melted and recast into a cylinder which has a base with radius 1.2 cm. Find the height of the cylinder. (3)
- c. The marks of 100 students in a particular test is given below. Draw a histogram for the given distribution and locate its mode. (4)

Marks	20 – 29	30 – 39	40 – 49	50 – 59	60 – 69
No. of students	18	23	32	16	11

VI

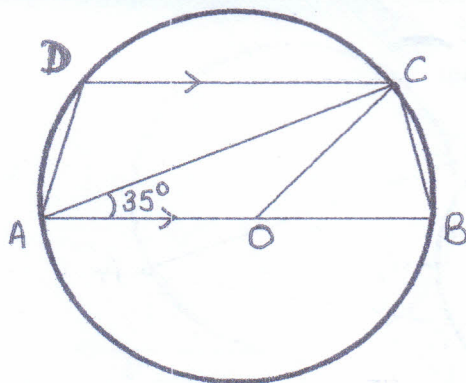
- a. Evaluate $\begin{bmatrix} 4 \cos 60^\circ & 2 \sin 30^\circ \\ \sin 90^\circ & 2 \cos 0^\circ \end{bmatrix} \begin{bmatrix} 1 & -2 \\ 3 & 1 \end{bmatrix}$ (3)
- b. Find the ratio in which the line segment joining $P(2, -5)$ and $Q(-3, 10)$ is divided by the Y-axis. Also find the point of intersection. (3)
- c. A model of a ship is made to a scale of 1:3000 (4)
- (i) If the length of the model is 40 cm, find the length of the ship in m.
 - (ii) If the area of the deck of the ship is 36 km^2 find the area of the deck of the model in m^2 .
 - (iii) If the volume of the model is 1.6 m^3 find the volume of the ship.

VII

- a. Riya bought a certain number of books for Rs.360. When the price of each Book was reduced by Rs.3, she could buy 6 more books for the same cost of Rs.360. Find the original cost of the book. (3)

...4/-

- b. A sphere of radius 12 cm is melted to form smaller cones of radius 8 cm and height 4 cm. Calculate the number of cones formed. (3)
- c. In the figure drawn below O is the centre of the circle. ABCD is a cyclic quadrilateral, $AB \parallel CD$ and $\angle CAB = 35^\circ$. Find $\angle COB$, $\angle ADC$, $\angle DAC$ and $\angle DCB$ (4)



VIII

- a. Solve the following quadratic equation and express your answer correct to 2 significant figures. (3)
- $$5x^2 + 10x - 3 = 0$$
- b. If $(x - 8)$, $(x + 4)$ and $(x + 28)$ are in continued proportion, then find the numbers. (3)
- c. Plot $A(2, 3)$, $B(5, 0)$ and $C(2, -3)$ on a graph paper. (4)
- Reflect A , B & C in Y -axis to get A' , B' , C' write their co-ordinates.
 - Name the figure $ABCC'B'A'$
 - Name any one invariant point on the figure.

IX

- a. The marks obtained by some students in a particular test are given below (6)

Marks	0 - 10	10 - 20	20 - 30	30 - 40	40 - 50	50 - 60	60 - 70	70 - 80	80-90	90-100
No. of students	4	10	16	21	27	19	10	6	4	3

- Draw an ogive for the above distribution, use your ogive to estimate
- Median
 - Upper Quartile
 - Number of students who scored above 65 marks
 - Number of students who scored less than 30 marks.
- b. From the top of a building 18 m high the angle of elevation of the top of another building on the opposite side of the street is 30° , and the angle of depression of the foot of the same building is 60° Find (4)
- The height of the other building
 - Distance between the two buildings